

TREND

WRITERS

Electric Charge and field -

1. Electricity - Electricity is the energy due to which substance have the property of attracting the light bodies.

2. Charge bodies - The bodies which have the property of attracting the light bodies are said to be charged or electrified.

3. Static Electricity - If the electricity so produced is kept stationary, it is called static electricity.

4. frictional electricity - The electricity produced on rubbing two the two objects which touch each other is called frictional electricity.

5. Charge - It is physical property of matter that cause property of it to exert force when place in electromagnetic field.

S.I unit of charge is coulomb. It is denoted by C.

The value of charge - 1.6×10^{-19} C.

Charge are two kinds -

1. Positive charge - when glass rod rubbed with silk charge on glass rod is called positive charge.

The bodies body which losses electron to the another body becomes positive charge.

2. Negative charge - The body which gains electrons from other body becomes negatively charge.

when ebonite rod rubbed with fur the charge on ebonite rod is called negative charge.

Conductor - Materials that allow electricity to pass through them are called conductor they have large number of free electricity.

Ex - Silver, copper, aluminium, human body.

Materials that do not allow electricity to pass through them are called Insulators. They have very small no. of free electrons.
Ex - wood, rubber, glass, etc.

• Methods of charging -

1. By conduction - In charging by conduction if charge body is touched with uncharged body so that the uncharged body get same kind of charge from the charged body by sharing on separation of two body they have same kind of charge.
2. By induction - In the process of ~~partial~~ induction an opposite charge is induce on the nearer end and the similar charge on the further end of uncharged conductor. In the presence of a charge body near by it thus ~~is~~ ^{is} electrostatically induced by the charged body but separation of charges take place.

Conservation of charge - The charge can neither be created nor it can destroyed this is the law of conservation of charge.

Ex - when a glass rod is rubbed with silk the amount of positive charge gain by the glass rod is equal to the amount of negative charge gain by the silk.

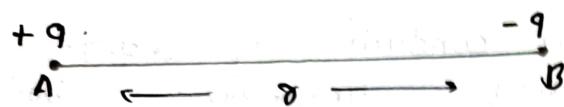
Quantization of charge - Quantization of charge states that the charge on the body is an integral multiple of the elementary charge.

$$Q = \pm Ne$$

where $N = 1, 2, 3, 4$

thus on a charged body total charge can be $\pm e, \pm 2e, \pm 3e$ nobody can have a charge $1.5e$ or $0.9e$, $-1.2e$.

~~Coulomb's Law~~ - The force of attraction between two point charges is proportional to the product of the magnitude of two charges and inversely proportional to the square of the distance between them.



$$F \propto q_1 q_2 \quad (I)$$

$$F \propto \frac{1}{r^2} \quad (II)$$

by eq (I) and (II)

$$F \propto \frac{q_1 q_2}{r^2}$$

$$F_2 \propto \frac{q_1 q_2}{r^2}$$

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$$F = 9 \times 10^9 \frac{q_1 q_2}{r^2}$$

Newton.

Unit Charge - If the force of attraction or repulsion between two point charges is 9×10^9 N/m² and 1m is the distance between them then the charge is called unit charge.

$$F = 9 \times 10^9 \text{ N/m}^2, q_1 q_2 = 1, r = 1 \text{ m}$$

$$9 \times 10^9 = 9 \times 10^9 \frac{q_1 q_2}{r^2}$$

$$q_2 = 1$$

$$q = \pm 1$$

~~Limitation of Coulomb's Law~~ -

If it is true only for points charges.

This is true for charges at rest.

This is true for long distance.

Compare Electric and Gravitational force.

Electric

- It is active over a volume.
- It obeys the inverse square law.
- It is conservative.
- It is central force.

Dissimilarities -

- It is much stronger.
- It is affected by the presence of medium.

Permittivity - The ability of substance to store electrical energy in a electric field.

Electric field - The region around an electric charge in which the electric force can be experienced is called the electric field.

Intensity of electric field - The force acting on a unit positive charge placed at any point in electric field. It is a vector quantity.

Electric field due to a point charge -

$$\vec{E} = \frac{q}{4\pi\epsilon_0 r^2} \hat{r}$$

$E = \frac{kq}{r^2}$

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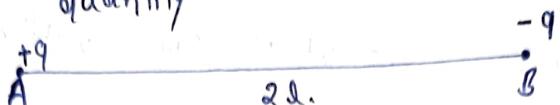
$E = \frac{kq}{r^2}$

$$E = \frac{kq}{r^2}$$

~~Electric dipole~~ - If there are two charges at a small distance between them this system is called an electric dipole.

Dipole moment - The product of value of either charge and distance between two charges is called dipole moment. It is denoted by p. It is

a vector quantity.



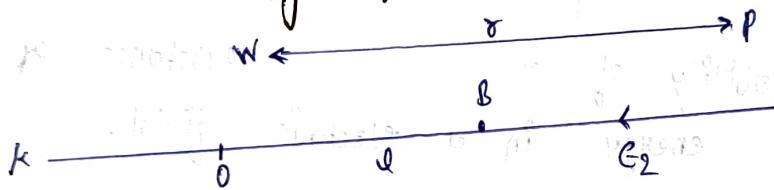
$$p = q \times 2d$$

S.I. unit = Cm

$$\text{D.R.} = [M^0 L^1 T^1 A^2]$$

Ex- H₂O, NH₃, HCl etc.

Electric field due to an electric dipole in end on position



Electric field intensity at the point P due to charge +q

Electric field intensity at the point P due to charge -q

$$E_1 = \frac{1}{4\pi\epsilon_0} \frac{q}{BP^2} \quad [K=1]$$

$$E_1 = \frac{1}{4\pi\epsilon_0} \frac{q}{(r-l)^2}$$

Electric field intensity at the point P due to charge -q

$$E_2 = \frac{1}{4\pi\epsilon_0} \frac{q}{AP^2}$$

$$E_2 = \frac{1}{4\pi\epsilon_0} \frac{q}{(r+l)^2}$$

Total electric field intensity.

$$E = E_1 - E_2$$

$$= \frac{1}{4\pi\epsilon_0} \frac{q}{(r-l)^2} - \frac{1}{4\pi\epsilon_0} \frac{q}{(r+l)^2}$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{1}{(r-d)^2} - \frac{1}{(r+d)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{(r+d)^2 - (r-d)^2}{(r^2 - d^2)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{r^2 + d^2 + 2rd - (r^2 + d^2 - 2rd)}{(r^2 - d^2)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \left[\frac{r^2 + d^2 + 2rd - r^2 - d^2 + 2rd}{(r^2 - d^2)^2} \right]$$

$$= \frac{q}{4\pi\epsilon_0} \frac{4rd}{(r^2 - d^2)^2}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{4qrd}{(r^2 - d^2)^2}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{2r \cdot 2qd}{(r^2 - d^2)^2}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{2pr}{(r^2 - d^2)^2}$$

$$\approx d \ll r$$

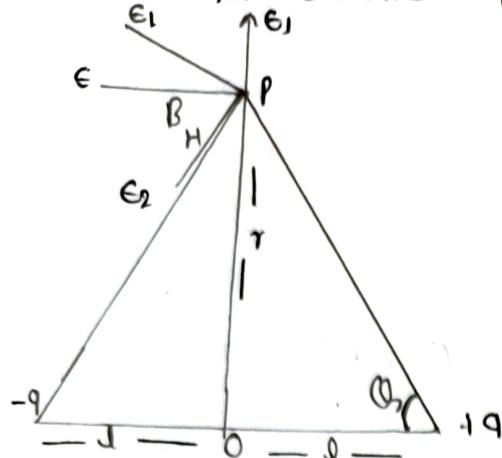
$$= \frac{1}{4\pi\epsilon_0} \frac{2pr}{(r^2)^2}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{2pr}{r^4}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{2p}{r^3} \quad N/C$$

~~Electric field due to a dipole in broadside on~~

C OM transverse position.



$$P \longrightarrow +q$$

$$\epsilon_1 = \frac{1}{4\pi\epsilon_0 k} \frac{q}{BP^2} \quad [k=2]$$

$$\epsilon_2 = \frac{1}{4\pi\epsilon_0 k} \frac{q}{AP^2} \quad (k=1)$$

$$AP^2 = BP^2 = r^2 + l^2$$

$$AP = BP = \sqrt{r^2 + l^2}$$

$$E = \epsilon_1 \cos\theta + \epsilon_2 \cos\phi$$

$$\cos\theta = \frac{B}{H} = \frac{l}{\sqrt{r^2 + l^2}}$$

$$\therefore [\epsilon_1 = \epsilon_2] \quad AP = BP$$

$$E = \epsilon_1 \cdot \epsilon_1 \cos\theta + \epsilon_1 \cos\phi$$

$$= 2\epsilon_1 \cos\theta$$

$$= 2 \times \frac{1}{4\pi\epsilon_0} \frac{q}{(r^2 + l^2)} \cdot \frac{l}{\sqrt{r^2 + l^2}}$$

$$= \frac{2}{4\pi\epsilon_0} \frac{l}{(r^2 + l^2)}$$

$$= \frac{2}{4\pi\epsilon_0} \frac{ql}{(r^2 + l^2)^{3/2}}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{2ql}{(r^2 + l^2)^{3/2}}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{P}{(r^2 + l^2)^{3/2}}$$

$l \ll r$

$$= \frac{1}{4\pi\epsilon_0} \frac{P}{(r^2)^{3/2}}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{P}{r^3}$$

3. Force and torque on a dipole in a uniform electric field -

$\tau = \text{one force} \times \text{perpendicular distance between two forces}$
 $= qE \times BC$

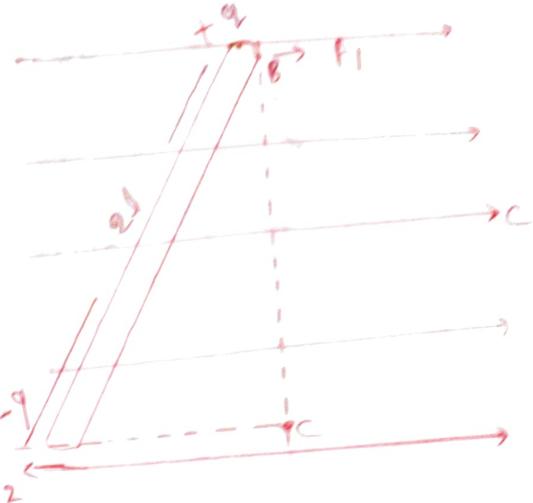
$$F = qE$$

$$\frac{F}{H} = \sin \theta$$

$$\frac{BC}{2l} = \sin \theta \Rightarrow BC = 2l \sin \theta$$

$$\tau = qE \times 2l \sin \theta$$

$$\tau = PE \sin \theta.$$



a. work done in turning a dipole -

$$\tau = PE \sin \theta$$

dipole $\rightarrow 0^\circ \rightarrow 0$

$$W = \int_0^\theta PE \sin \theta d\theta$$

$$W = PE_1 \int_0^\theta \sin \theta d\theta$$

$$W = PE \left[-\cos \theta \right]_0^\theta$$

$$W = PE \left[-\cos \theta - (-\cos 0) \right]$$

$$W = PE \left[-\cos \theta + 1 \right]$$

$$W = PE \left[1 - \cos \theta \right]$$

* work done in turning a dipole in an electric field

Case (1) $\theta = 90^\circ$

$$W = PE (1 - \cos 90^\circ) = PE$$

$$(1 - 1) = 0$$

Case (2) $\theta = 180^\circ$

$$W = PE [1 - \cos 180^\circ] = PE [1 - (-1)] \\ = 2PE.$$

Potential energy of dipole - $d\theta = \pi/2 \rightarrow 0^\circ$

$$C = PE \sin \theta$$

$$dU = 2 d\theta$$

$$= PE \sin \theta d\theta$$

$$U = \int_{\pi/2}^0 PE \sin \theta d\theta$$

$$U = PE \int_{\pi/2}^0 \sin \theta d\theta$$

$$= PE [-\cos \theta]_{\pi/2}^0$$

$$= PE [-\cos \theta - (-\cos \pi/2)]$$

$$= PE [-\cos \theta + 1]$$

$$= PE [1 - \cos \theta]$$

Cause (1)

$$\theta = 90^\circ$$

$$U = PE [1 - \cos 90^\circ]$$

$$PE [1 - 1]$$

$$= 0$$

Cause (2)

$$\theta = 180^\circ$$

$$U = PE [1 - \cos 180^\circ]$$

$$= PE [1 - (-1)]$$

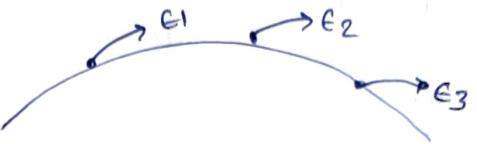
$$= 2PE$$

1. Linear charge density - If the charge is distributed continuously on a linear conductor the charge on its unit length is called the linear charge density. It is expressed by the letter λ . Its unit is Coulomb/meter. $\frac{C}{m}$

2. Surface charge density - If charge is distributed on the surface of the conductor then charge on unit area of conductor is called the σ . It is denoted by sigma.

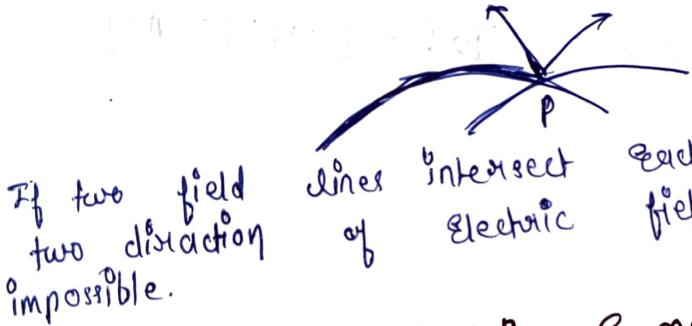
3. Volume charge density - If the charge is distributed over the entire volume of a conductor the charge is unit volume of conductor. Charge density is unit volume of conductor. It is denoted by ρ (rho). Its unit is Coulomb/meter³. $\frac{C}{m^3}$

Electric field lines - An imaginary linear or curved line from a point of an electric field such that tangents to it gives all the direction of the electric field at that point.



Properties -

- They are started from positive charge to ne. charge.
- They are the open curves.
- They are not present inside the conductor.
- They are always normal to the charge surface.
- They do not intersect each other.



If two field lines of two distinct electric fields intersect each other which will represent impossible.

Difference between electric & magnetic field lines -

Electric flux - The total passing through a electric flux. It is scalar quantity.

number of electric field lines in an electric field is called denoted by the letter Φ . It can be positive, negative, zero.

Electric field lines

- They are the open curves.
- They are always to the charged surface.
- They are not present inside the conductor.

Magnetic field lines.

There are the closed curves.

They are not essentially normal to the surface of magnet but they can be in any direction.

They are present inside the magnet also.

$$\int d\phi = \int \vec{E} \cdot \vec{ds}$$

$$e = \frac{f}{a}$$

$$\therefore \phi = e \cdot ds \text{ coll.}$$

$$\underline{\underline{\phi = e \cdot ds}}$$

$$\begin{aligned}\phi \cdot a &= 0^\circ \\ &= 0\end{aligned}$$

$$2. \quad \theta = 90^\circ$$

$$\phi = 0$$

$$Q = e \cdot ds$$

$$\frac{N}{C} \times m^2$$

$$\text{S.I. Unit} = Nm^2/C$$

$$DF = [ML^3T^{-3}A^{-1}]$$

Gauss Law

$$\phi_e = \frac{Q}{\epsilon_0}$$

$$e = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$$

$$d\phi = \vec{E} \cdot \vec{ds}$$

$$\int d\phi = \int \frac{1}{4\pi\epsilon_0} \frac{-Q}{r^2} \frac{ds}{r^2}$$

$$\phi = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \int ds$$

$$\frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \frac{4\pi r^2}{4\pi r^2}$$

$$\phi_e = \frac{Q}{\epsilon_0}$$

By the gauss theorem Coulomb inverse square law -

$$\Phi = \int \epsilon \cdot ds$$

$$= \epsilon \cdot \int ds$$

$$= \epsilon \cdot 4\pi r^2 \quad \text{--- (1)}$$

By Gauss law

$$\Phi = \frac{Q}{\epsilon_0} \quad \text{--- (1)}$$

by Eq (1) & (1)

$$\epsilon \cdot 4\pi r^2 = \frac{Q}{\epsilon_0}$$

$$\epsilon = \frac{1}{4\pi \epsilon_0} \frac{Q}{r^2}$$

$$E = \frac{F}{q}$$

$$F = E \cdot q$$

$$F = \frac{1}{4\pi \epsilon_0} \frac{Q \cdot q}{r^2}$$

Write electric field intensity due to uniformly charged thin spherical shell.

$$\Phi = \int \epsilon ds$$

$$= \epsilon \int ds$$

$$= \epsilon \cdot 4\pi x^2 \quad \text{--- (1)}$$

$$\Phi = \frac{q}{\epsilon_0} \quad \text{--- (1)}$$

By Eq (1) & (1)

$$E = \frac{1}{4\pi \epsilon_0} \frac{q}{x^2} \text{ N/C}$$

Cause - (2)

Cause - (1)

$$E = \frac{1}{4\pi \epsilon_0} \cdot \frac{q}{r^2}$$

$$E = \frac{1}{4\pi \epsilon_0} \frac{Q}{r^2}$$

$$E = 0,$$

Clefford's theory of origin of charge
Electrons are negatively charged particles.
Electrons are present in all matter.
Electrons are present in all matter.

Conductor

- A conductor allows current to flow easily through it.
- Electronic charge exists on the surface of conductor.
- The resistance of conductor is very low.
- The thermal conductivity (heat allowance) of a conductor is very high.
- Copper, aluminum and mercury are some conductors.
- Electrons move freely within the conductor.

Insulator

- Insulators don't allow current to flow through it.
- Electronic charges are absent in insulator.

The resistance of insulator is very high.

The thermal conductivity of an insulator is very low.

cocel, paper, and ceramic are some insulators.

Electrons do not move freely within the insulator.