



TREND

WRITERS

CHAPTER = 4

• Magnetic effect of electric current - The phenomenon of producing magnetic field around a conductor on passing current through it is called magnetic effect of electric current.

• Biot-Savart Law - An expression for the intensity of mag. field - field due to a current carrying conductor is known as Biot-Savart Law.

Let xy is a conductor of length l .

Consider a small element dl

The intensity of magnetic field dB - at a point P due to this element.

1. $dB \propto I$ — (i)
2. $dB \propto dl$ — (ii)
3. $dB \propto \sin \theta$ — (iii)
4. $dB \propto \frac{1}{r^2}$ — (iv)

by eq (i) (ii) & (iii) (iv)

$$dB = k \frac{I dl \sin \theta}{r^2}$$

$$dB = k \frac{I dl \sin \theta}{r^2} \quad k = \frac{\mu_0}{4\pi}$$

$$dB = \frac{\mu}{4\pi} \frac{I dl \sin \theta}{r^2}$$

$$dB = 10^{-7} \frac{I dl \sin \theta}{r^2}$$

$$\frac{\mu_0}{4\pi} = 10^{-7} \text{ tesla} \cdot \text{Ampere} \cdot \text{m}^{-1}$$

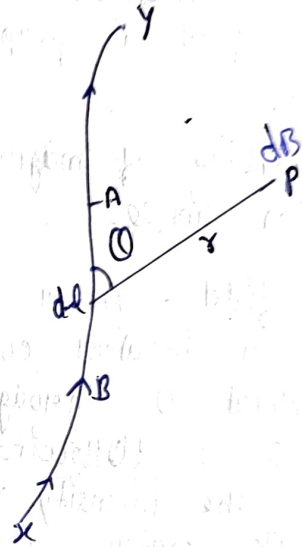
Unit constant.

$$dB = 10^{-7} \cdot dl = 1\text{m} \quad \theta = 90^\circ \quad r = 1\text{m}$$

$$10^{-7} = 10^{-7} \frac{I \times 1 \times \sin 90^\circ \times 1}{1^2}$$

$$\frac{10^{-7}}{10^{-7}} = I$$

$$\underline{\underline{I = 1}}$$



write difference betw. biot-savart law and coulombs law

Similarity -

1. It follows inverse square law
 2. In this magnetic field is a long range field.
 3. magnetic field is linear
- It follows inverse square law
 - In this electric field is a long range field.
 - magnetic field is linear

Dissimilarity -

1. magnetic field is produce due to vector source.
 2. magnetic field is perpendicular to plane.
 3. The magnitude of magnetic field depend on $\sin \theta$.
- electric field is produce due to scalar source.
 - electric field lies along the displacement.
 - The magnitude of electric field does not depend on the angle

* magnetic field - At a central of circular point carrying current.
 * Consider a circular coil of radius r with central O through which the current I is following in clockwise direction the intensity of magnetic field at its centre is to be determined.

* Biot - savart law - The magnetic field intensity at centre O due to element AB is given by.

$$dB = \frac{\mu_0}{4\pi} \frac{I dl \sin \theta}{r^2} \quad (\theta = 90^\circ)$$

$$dB = \frac{\mu_0}{4\pi} \cdot \frac{I dl}{r^2}$$

• Net intensity -

$$\int dB = \int \frac{\mu_0}{4\pi} \frac{I dl}{r^2}$$

$$B = \frac{\mu_0}{4\pi} \cdot \frac{I}{r^2} \int dl$$

$$B = \frac{\mu_0}{4\pi} \frac{I}{r^2} \cdot 2\pi r$$

$$dB = \frac{\mu_0}{4\pi} \frac{I dl \sin \theta}{r^2}$$

$$dB = \frac{\mu_0}{4\pi} \frac{I dl \sin \theta}{r^2}$$

$$B = \frac{\mu_0}{4\pi} \frac{2\pi I}{r} = \frac{\mu_0 I}{2r}$$

If the no. of turns is n

$$B = \frac{\mu_0 n I}{2r} \text{ Tesla}$$

* Magnetic field at a point on the axis of circular coil loop carrying current.

Consider a circular coil of radius small a with center O let the current I is flow in the direction of arrow at a point P at a distance from center O . The intensity of magnetic field is to be determined suppose AB and $A'B'$ are two opposite small

Elements. The intensity of magnetic field at point P due to small element AB .

$$dB = \frac{\mu_0}{4\pi r^2} I dl \sin \alpha$$

$$\alpha = 90^\circ$$

$$dB = \frac{\mu_0}{4\pi} \frac{I dl}{r^2}$$

at point P the intensity of magnetic field dB can be dissociated in two components.

- (I) $dB \cos \alpha$ along PN
- (II) $dB \sin \alpha$ along the OP .

The intensity of magnetic field due to small element $A'B'$

$$dB = \frac{\mu_0}{4\pi} = \frac{I dl}{r^2}$$

Again dB dissociate in two components.

- (I) $dB \cos \alpha$ along PN'
- (II) $dB \sin \alpha$ along OP .

PN and PN' are equal magnitude & opposite direction so they will cancel each other.

The intensity of magnetic field due to circular loop at point P .

$$B = \int dB \sin \alpha$$

$$= \int \frac{\mu_0}{4\pi} \cdot \frac{I dl}{r^2} \sin \alpha$$

$$\text{But, } \sin \alpha = \frac{a}{r}$$

II ~~Zero~~ Second Cause -

If point P lies at a distance large to radius of loop

$$dB = \frac{\mu_0 I n a^2}{2 (\pi^2)^{3/2}}$$

$$dB = \frac{\mu_0 I n^2}{2r^3} \text{ tesla.}$$

Factors affecting the magnetic field at the central of circular coil carrying current.

$$B = \frac{\mu_0 n I}{2r}$$

1. No. of turns in the coil - On increasing the no. of turns of the coil the intensity of magnetic field also increases.
2. Current flowing through the coil - If the value of current flowing through the coil increases intensity of magnetic field also increases.
3. Radius of the coil - If the radius of coil is small the intensity with more of magnetic field depends on permeability of medium - The intensity of magnetic field depends on permeability of medium.

~~Explain~~ Explain and derive Ampere's law -

Ampere's law - According to this law line integral of magnetic field vector lies over the closed loop in vacuum is μ_0 time the current in cross by loop.

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

Consider an infinite long straight conductor carrying current I from Biot-Savart law the magnetic field vector due to current carrying conductor at a point distant r is given by

$$B = \frac{\mu_0 I}{2\pi r}$$

Ampere's law -

$$\oint \vec{B} \cdot d\vec{l} = \oint B dl \cos \theta$$

$\theta = 0$

$$\oint B dl$$

$$B \oint dl$$

$$B \oint dl$$

$$\frac{\mu_0 I}{2\pi r} \cdot 2\pi r$$

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I \text{ tesla}$$

~~•~~ Magnetic field near a wire carrying current, why?

By ampere's law.

Consider an infinite long wire conductor carrying current I .

According to ampere's law

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

$$\oint B dl \cos \theta = \mu_0 I$$

$\theta = 0$

$$\oint B dl = \mu_0 I$$

$$B \oint dl = \mu_0 I$$

$$B \cdot 2\pi r = \mu_0 I$$

$$B = \frac{\mu_0 I}{2\pi r} \text{ tesla.}$$

~~•~~ Magnetic field due to a long current carrying wire.

Let wire be an infinite having n number of turns per unit length and current I is flowing through it when current is flow through the solenoid it behaves like a bar magnet uniform magnetic field is inside the solenoid and it is almost the zero outside the solenoid.

at magnetic field for the rectangle ABCD. know line integral

$$\oint \vec{B} \cdot d\vec{l} = \int_a^b \vec{B} \cdot d\vec{l} + \int_b^c \vec{B} \cdot d\vec{l} + \int_c^d \vec{B} \cdot d\vec{l} + \int_d^a \vec{B} \cdot d\vec{l}$$

$$= \int_a^b B dl \cos 0^\circ + \int_b^c B dl \cos 90^\circ + \int_c^d B dl \cos 180^\circ + \int_d^a B dl \cos 270^\circ$$

$$\oint \vec{B} \cdot d\vec{l} = B \int_a^b dl + 0 + 0 + 0$$

(for $\cos \theta = 0$)

By Ampere's law

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 n I r \quad \text{--- (1)}$$

By eq (1) & (11)

$$B r = \mu_0 n I r$$

$$B = \mu_0 n I \text{ tesla}$$

Force acting on a moving charge in a magnetic field then when a charge q moves in a magnetic field then a force the magnitude of force acting on a moving charge in magnetic field is.

- Directly proportional to the magnitude of the magnetic field
- Directly proportional to the intensity of magnetic field
- Proportional to the velocity of charge $F \propto v$
- Proportional to the $\sin \theta$ where θ is angle between v & B

$$F \propto B$$

$$F \propto v$$

$$F \propto \sin \theta$$

by eq (I) (II) & (III) (IV)

$$F \propto qvB \sin \theta$$

$$F = k qvB \sin \theta$$

in S.I system $k=1$

$$F = qvB \sin \theta \text{ newton}$$

Case (I)	Case (II)	Case (III)
$v = 0$	$\theta = 0^\circ / 180^\circ$	$\theta = 90^\circ$
$F = 0$	$F = qvB \sin \theta$	$F = qvB \sin 90^\circ$
	$F = 0$	$F = qvB$ maximum

force btw to current carrying conductor - consider to long straight conductor AB and CD had parallel to each other at distance d current I_1 is flowing through the conductor AB the mag magnetic field at a distance d will be

$$B = \frac{\mu_0}{4\pi} \frac{2I_1}{d}$$

If I_2 to I_3 made to flow through the conductor CD the force action on its length l will be.

$$F_2 = I_2 B_1 \sin \theta$$

$$= I_2 B_1 \sin 90^\circ$$

$$F = I_2 B_1 l$$

by eq (1)

$$F_2 = I_2 \frac{\mu_0}{4\pi} \frac{2 I_1 l}{d}$$

$$F_2 = \frac{\mu_0}{4\pi} \frac{2 I_1 I_2 l}{d}$$

force acting on conductor CD per unit length will be.

$$F = \frac{F_2}{l} = \frac{\mu_0}{4\pi} \frac{2 I_1 I_2}{d} \text{ N/m.}$$

- It can be proved that the force acting on conductor AB per unit of length will be same as CD.

* Direction of force - If the direction of current in both left hand rule) the force acting on CD towards the conductor AB.
If the direction of current is opposite by (Fleming's left hand rule) the force acting on ~~CD~~ and AB will be repel each other.

- If we stage four finger middle finger and the thumb of our left hand in mutually perpendicular direction such that four finger point along the direction of magnetic field the middle finger point along the direction of current than thumb will be in the direction of force.

* Torque on a current carrying coil in a uniform magnetic field. When ever a current is made to pass through a coil placed in a uniform magnetic field then a torque acts on it which rotates the coil and tries to make it perpendicular to the direction of field.

Suppose PQRS is a rectangular coil which is suspended in uniform magnetic field. Let the length of coil

$$PQ = RS = d$$

and breadth $PR = SP = b$ force acting on current carrying side SP will be

$$\vec{F}_1 = I (\vec{B} \times \vec{SP})$$

Similarly the force on side QR will be

$$\vec{F}_2 = I (\vec{B} \times \vec{QR})$$

The two forces F_1 and F_2 having same line of action but their direction is opposite so they will be cancel each other.

The forces action of side PQ

$$\vec{F}_3 = I (\vec{B} \times \vec{PQ})$$

The force acting on side TR will be

$$\vec{F}_4 = I (\vec{B} \times \vec{TR})$$

The force is F_3 and F_4 are equal in magnitude and in opposite direction but along different line of action hence the pair of force produce turning effect this is called torque force.

• Torque magnitude of either force into perpendicular distance b/w the line of action.

$$\begin{aligned} \text{Torque} &= b \cdot d \cdot \sin \theta \\ &= I A B \sin \theta \end{aligned}$$

$$\sin \theta = \frac{OP}{SP}$$

$$\begin{aligned} OP &= SP \sin \theta \\ &= b \sin \theta \end{aligned}$$

$$Z = I B l \times b \sin \theta$$

$$= I B A \sin \theta$$

$$Z = N I A B \sin \theta$$

If N is no. of turns in the coil then $Z = N I A B$.

Case (I)

$I B l - \perp O$
In ΔPOS

$$\sin 90^\circ = \frac{PO}{SP}$$

$$PO = SP \cdot b$$

$$Z = I B P \times b$$

$$= I B A$$

$$Z = N I A B$$

Case (II)

$I B l - \perp O$
In ΔPOS

$$\sin \theta = \frac{PO}{SP}$$

$$PO = SP \cdot \sin \theta$$

$$= b \sin \theta$$

$$Z = I B P \times b \sin \theta$$

$$= I B A \sin \theta$$

$$Z = N I A B \sin \theta$$

Case (III)

$I B l - \perp O$

In ΔPOS

$$\sin \theta = \frac{PO}{SP}$$

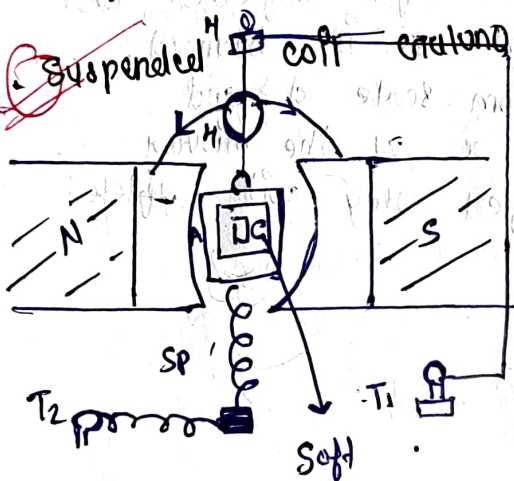
$$PO = SP \cdot \sin \theta$$

$$= b \sin \theta$$

$$Z = I B P \times b \sin \theta$$

$$= I B A \sin \theta$$

$$Z = N I A B \sin \theta$$



meter -

Construction - Suspended coil galvanometer is such that the coil is made of copper wire wound on a soft iron core. The coil is fixed with a spiral spring and a soft iron wire. The coil is free to rotate.

The coil is suspended between the poles.

When a magnetic field is applied, a torque is exerted on the coil. This torque is called deflection torque. This is given by

$$Z = \frac{N I}{A B}$$

Let ϕ be the twist produced in the spring due to rotation of the coil. The restoring torque per twist is k .

Restoring (R)

Deflecting (D)

Torque = $\frac{\text{force} \times \text{perpendicular distance}}{\text{perpendicular}}$

$$NIA \quad B = \frac{k \phi}{NAB}$$

$$I = \frac{k}{NAB} \phi$$

when $n = \frac{k}{NAB}$ which is called
galvanometer constant.

$$I = n \phi$$

$$I \propto \phi$$

the deflection of coil is directly proportional to the current flowing through it.

~~working~~ principle of moving coil galvanometer. The base of galvanometer is made horizontal with the help of leveling screws. The connecting screws T_1 and T_2 are connected with external circuit. The current flows through the coil and it gets deflected and after some time it stops when it is balanced. Let the distance of mirror from scale be d and deflection of light on the scale is x . If the mirror is deflected by $\Delta \phi$ then the reflected ray will be deflected by 2ϕ .

$$\tan \theta = \frac{x}{d}$$

ϕ is very small

$$2\phi \approx \frac{x}{d}$$

$$\phi \approx \frac{x}{2d}$$

$$\phi \propto x$$

$$\phi \propto I$$

$$I \propto x$$

• coil marks and demerits of moving coil galvanometer.

- merits - It is very sensitivity so passing very small current can be measured with help of it.
- Demerits - before use its needs needs leveling.
- The coil is suspended with the help of ~~string~~ staple which may give
 - It is not easy for portable

* sensitivity of galvanometer. - A galvanometer is said to be more sensitive if on passing very small current or on applying very small voltage the coil deflect more.

1. current sensitivity - $\frac{\phi}{I} = \frac{nBA}{k}$

current sensitivity $S_i = \frac{nBA}{k}$

2. voltage sensitivity - $S_v = \frac{\phi}{V} = \frac{\phi}{IR}$

$S_v = \frac{\phi}{IR} = \frac{nBA}{kR}$

$S_v = \frac{nBA}{kR}$

$S_v = \frac{S_i}{R}$

- For ~~sensitivity~~ sensitive galvanometer -
- n should be greater no. of turns should be more
- B should be large magnetic should be strong mag.
- A should be large coil should be large.
- k should be small. Copy sent ~~significance~~ significance.