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CHAPTER 7

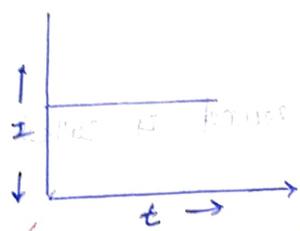
Current - The rate of flow of charges is call electric current

Electric current mainly have two type -

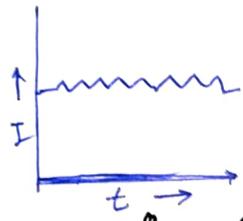
* Direct current - Direct current is that electric current whose direction does not change with time whether its magnitude changed or not.

DC current - Current can be classified into two type

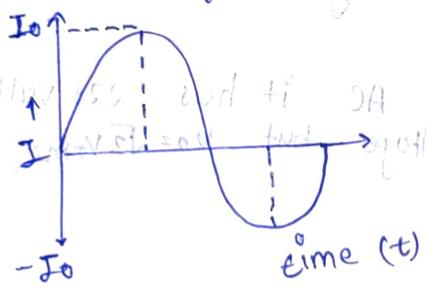
• Steady DC - Steady DC is that DC which remains constant both in magnitude and direction.



• Varying DC - The dc whose magnitude always changes with time but direction remain constant.



• Alternating current - That current whose direction and magnitude both changes with time



It is denoted by $I = I_0 \sin \omega t$

Alternating EMF - All Alternating voltage that voltage whose magnitude and direction change with time period periodically. It is denoted by $e = E_0 \sin \omega t$

Same value of voltage and current for same power

I - Initial current

I_0 - Peak value

ω - Angular frequency

• Voltage - The potential difference between any two points is called Voltage

It is denoted by $V = V_0 \sin \omega t$

• Amplitude peak - The maximum value of alternating current in any direction is called its amplitude, or peak value.

$I = I_0 \sin \omega t$ where I_0 is amplitude or peak value.

• Time period or periodic time - The time taken by alternating current to complete its one cycle is called time period or periodic time

$$T = \frac{2\pi}{\omega}$$

• Frequency - Number of cycles completed by AC in one second is called frequency.

It is denoted by ν .

$$\nu = \frac{1}{T}$$

$$= \frac{1}{\frac{2\pi}{\omega}}$$

$$\nu = \frac{\omega}{2\pi}$$

$$\omega = 2\pi\nu$$

~~The~~ AC of same voltage is more dangerous than DC why?

The current supplied in house is AC it has 220 voltage it is the RMS value of AC voltage but $V_0 = \sqrt{2} V_{rms}$

$$V_0 = \sqrt{2} V_{rms}$$

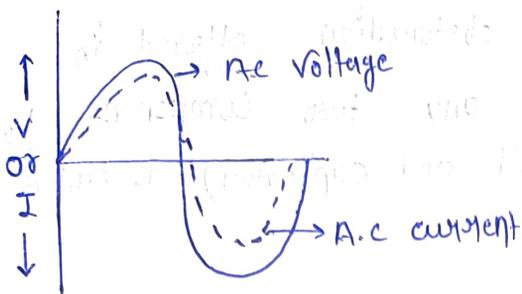
$$\sqrt{2} \times 220$$

$$= 1.41 \times 220$$

$$= 3.11 \text{ voltage}$$

Thus the peak value of AC voltage 220 volt is ~~220~~ 311 volt if the voltage value of DC 220 V then it will remain same so it is clear that the AC of same voltage is more dangerous than DC.

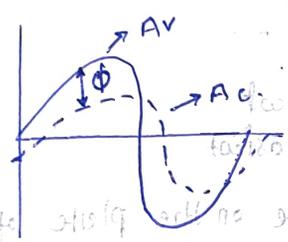
Phase difference between voltage and current.
 (i) When both current voltage is same phase.



$$V = V_0 \sin \omega t$$

$$I = I_0 \sin \omega t$$

(II) when voltage is leading - (अग्र)

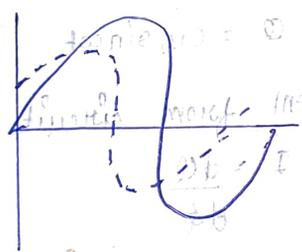


$$V = V_0 \sin (\omega t + \phi)$$

$$I = I_0 \sin \omega t$$

$$I = I_0 \sin (\omega t - \phi)$$

(III) when current is leading -

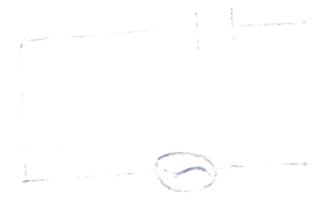


$$V = V_0 \sin \omega t$$

$$I = I_0 \sin (\omega t + \phi)$$

$$V = V_0 \sin (\omega t - \phi)$$

$$I = I_0 \sin \omega t$$



Define resistance, reactance, and impedance in the path of AC.

Resistance - The obstruction offered by the conductor in the path of AC alternating current is called resistance of the conductor. It is denoted by R and its unit is Ω .

Reactance - In a AC circuit the opposition offered by induction coil or capacitor in the path of AC is called reactance. It is denoted by X its unit is Ω . The reciprocal of reactance is called susceptance its unit is Ω^{-1} .

Reactance is in two types

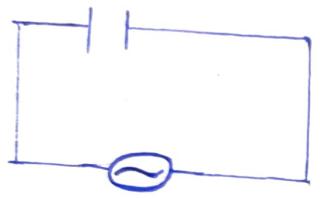
(i) **Inductive Reactance** - The obstruction offered in the path of AC by Inductance coil is called inductive reactant. It is denoted by X_L .

Capacitive reactance - The obstruction of AC by capacitor is called capacitive reactance. It is denoted by X_c

Impedance - In AC circuit the obstruction offered in the path of ac by any two component the group (resistance, inductance coil and capacitor) is called Impedance - it is denoted by Z Its unit Ω

The reciprocal of Impedance admittance is unit is Ω^{-1}

AC circuit containing only Pure capacitance -



$v = v_0 \sin \omega t$
 $v = v_0 \cos \omega t$

Charge on the plate of capacitor

$Q = CV$

$Q = C v_0 \sin \omega t$

Current from circuit

$I = \frac{dQ}{dt}$

$= \frac{d}{dt} (C v_0 \sin \omega t)$

$= C v_0 \frac{d}{dt} \sin \omega t$

$= \omega C v_0 \cos \omega t$

$I = \omega C v_0 \sin \left(\frac{\pi}{2} + \omega t \right)$

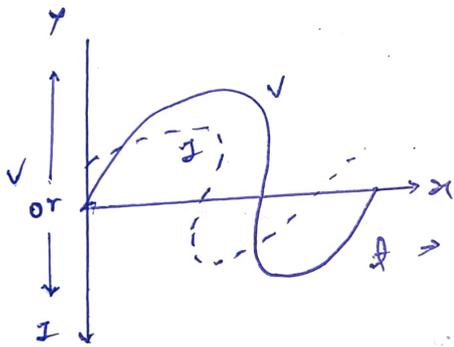
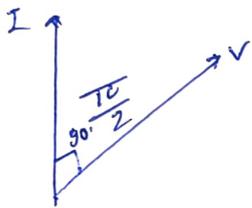
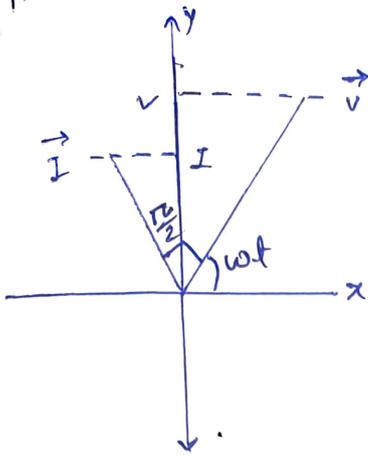
but

$I = I_0 \sin \left(\frac{\pi}{2} + \omega t \right)$

$I_0 = \omega C v_0$

Peak value of current.

Phasor diagram



- AC circuit containing only pure inductance -
 Consider a capacitor of capacitance C is connected with an A.C. source applied voltage is given by.

$$v = V_0 \sin \omega t$$

Charge on the plate of capacitors

$$Q = CV$$

$$Q = CV_0 \sin \omega t$$

Current from circuit

$$I = \frac{dQ}{dt}$$

$$= \frac{d}{dt} (CV_0 \sin \omega t)$$

$$CV_0 \omega \cos \omega t$$

$$I_0 = \omega CV_0$$

$$\frac{1}{\omega C} = \frac{V_0}{I_0}$$

but $\frac{V}{I} = R$

$$R = \frac{1}{\omega C}$$

$$X_c = \frac{1}{\omega C}$$

$$X_c = \frac{1}{2\pi \nu C}$$

$$\frac{t}{\omega C} = X$$

$$\frac{t}{2\pi \nu C} = X$$

$$I = I_0 \cos \omega t$$

$$I = I_0 \sin \left(\frac{\pi}{2} + \omega t \right)$$

but $I = I_0 \sin \left(\frac{\pi}{2} + \omega t \right)$

then $I_0 = \omega C V_0$
Peak value of current

Phasor diagram -

$$I_0 = \omega C V_0$$

$$\frac{I}{\omega C} = \frac{V_0}{I_0}$$

but $\frac{V}{I} = R$

$$R = \frac{1}{\omega C}$$

$$X_C = \frac{1}{\omega C}$$

$$X_C = \frac{1}{2\pi f C}$$



AC circuit containing only pure inductance -

Let a coil of inductance L has been connected with AC source.

Voltage applied on inductance coil is given by

$$V = V_0 \sin \omega t \quad (1)$$

then e.m.f is generated on coil

$$e_s = -L \frac{dI}{dt}$$

So instantaneous voltage

$$V = L \frac{dI}{dt}$$

Since Resistance = 0

$$V = -L \frac{dI}{dt} = 0$$

$$V = L \frac{dI}{dt}$$

$$V_0 \sin \omega t = \frac{L dI}{dt}$$

$$\frac{dI}{dt} = \frac{V_0}{L} \sin \omega t$$

$$\int \frac{dI}{dt} = \frac{V_0}{L} \int \sin \omega t$$

$$I = \frac{V_0}{L} \left(-\frac{\cos \omega t}{\omega} \right)$$

$$= -\frac{V_0}{\omega L} \cos \omega t$$

$$I = \frac{V_0}{\omega L} \sin \left(\frac{\pi}{2} - \omega t \right)$$

$$I = \frac{V_0}{\omega L} \sin \left(\frac{\pi}{2} - \omega t \right)$$

$$I = \frac{V_0}{\omega L} \sin \left(\omega t - \frac{\pi}{2} \right)$$

$$I = I_0 \sin \left(\omega t - \frac{\pi}{2} \right)$$

• phase or - diagram -

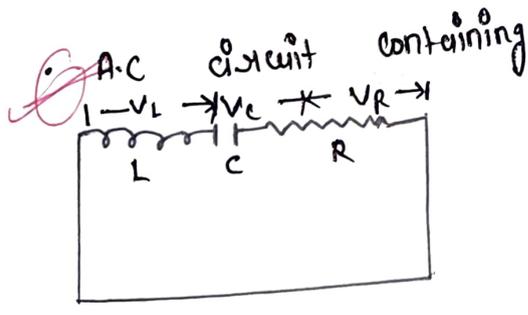
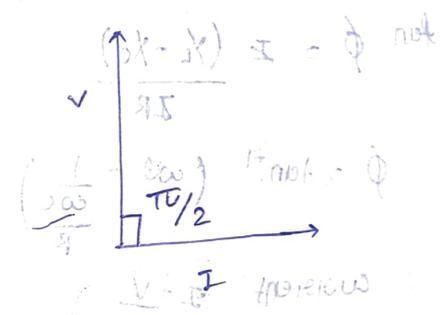
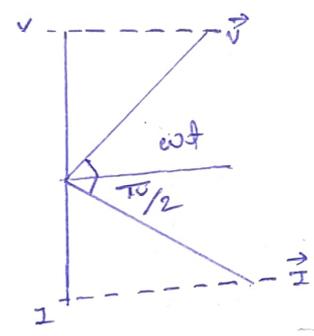
$$I_0 = \frac{V_0}{\omega L}$$

$$\frac{V_0}{I_0} = \omega L$$

$$\text{but } \frac{V}{I} = R$$

$$X_L = \omega L$$

$$X_L = 2\pi \nu L$$



Inductance Capacitance and Resistance -

Let inductance L capacitance C and Resistance R connected in series in A.C circuit

Voltage in given by $V = V_0 \sin \omega t$

Resultant voltage

$$V_C = IX_C$$

$$V_R = IR$$

$$V_L = IX_L$$

$$V_2 = VR^2 + (V_L - V_C)^2$$

$$V = \sqrt{VR^2 + (V_L - V_C)^2}$$

Squaring both sides and substituting the values

$$V^2 = I^2 R^2 + (IX_L - IX_C)^2$$

$$V^2 = I^2 [R^2 + (X_L - X_C)^2]$$

$$V = I \sqrt{R^2 + (X_L - X_C)^2}$$

$$V = I \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

$$\frac{V}{I} = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

$$\text{Impedance } Z = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

* Phase difference -

$$\tan \phi = \frac{V_L - V_C}{V_R}$$

$$= \frac{IX_L - IX_C}{IR}$$

$$\tan \phi = \frac{X_L - X_C}{R}$$

$$\phi = \tan^{-1} \left(\frac{\omega L - \frac{1}{\omega C}}{R} \right)$$

$$\text{Current } I = \frac{V}{Z}$$

$$I_0 = \frac{V_0}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}}$$

• Resonant Condition -

$$X_L = X_C$$

$$\omega L = \frac{1}{\omega C}$$

$$\omega^2 = \frac{1}{LC}$$

$$\omega = \frac{1}{\sqrt{LC}}$$

$$2\pi \nu = \frac{1}{\sqrt{LC}}$$

The current flowing through LCR circuit attains maximum value for a specific frequency this is called the state of resonance and this frequency is known as resonant frequency.

Power in alternating current circuit -

The value of energy spend in any circuit is called its power in alternating current circuit the value of voltage and current change with time so, the instantaneous power is define as.

instantaneous power = instantaneous voltage

$v = v_0 \sin \omega t$

$I = I_0 \sin (\omega t - \phi)$

ϕ is phase difference betw v and I

$P = VI$

$= v_0 \sin \omega t \cdot I_0 \sin (\omega t - \phi)$

$= \frac{1}{2} v_0 I_0 [2 \sin \omega t \sin (\omega t - \phi)]$

$[2 \sin A \sin B = \cos (A-B) - \cos (A+B)]$

$\frac{1}{2} v_0 I_0 \cos (\omega t - \omega t - \phi) - \cos (\omega t + \omega t + \phi)$

$\frac{1}{2} v_0 I_0 [\cos \phi - \cos (2\omega t - \phi)]$

$\frac{1}{2} v_0 I_0 \cos \phi - \frac{1}{2} v_0 I_0 \cos (2\omega t - \phi)$

In complete cycle Average value of $\cos (2\omega t - \phi)$ is 0.

$= \frac{1}{2} v_0 I_0 \cos \phi$

$P = \frac{v_0}{\sqrt{2}} \cdot \frac{I_0}{\sqrt{2}} \cos \phi$

$P_{av} = V_{rms} \cdot I_{rms} \cos \phi$

Special case -

I - AC circuit contains only atomic resistance than phase difference = 0

$P_{av} = V_{rms} \times I_{rms} \times \cos \phi$

$= V_{rms} \times I_{rms} \times \cos 0$

$$P_{av} = V_{rms} \times I_{rms} \quad (1)$$

Thus maximum energy consumed

$$I_{rms} = \frac{V_{rms}}{R}$$

or eq - (1)

$$P_{av} = V_{rms} \times \frac{V_{rms}}{R}$$

$$P_{av} = \frac{V_{rms}^2}{R}$$

$$= \frac{(I_{rms} R)^2}{R}$$

$$P_{av} = I_{rms}^2 R$$

$$= \left(\frac{I_0}{\sqrt{2}} \right)^2 R$$

$$= \frac{I_0^2}{2} R$$

$$I_0 = I_{rms} \sqrt{2}$$

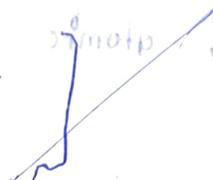
$$I_{rms} = \frac{I_0}{\sqrt{2}}$$

II Special case

II ac circuit contains only Inductor capacitor

$$\cos(-\theta) = \cos \theta$$

$$\phi = \frac{\pi}{2}$$



$$\phi = \frac{-\pi}{2}$$

$$= \frac{-\pi}{2}$$

$$P_{av} = V_{rms} \times I_{rms} \times \cos \phi$$

$$= V_{rms} \times I_{rms} \times \cos \frac{\pi}{2}$$

$$= 0$$

III Special case -
a-c circuit contains L and R in series -

$$\tan \phi = \frac{\omega L - \frac{1}{\omega C}}{R}$$

By P.C.T

$$H^2 = A^2 + B^2$$

$$\cos \phi = \frac{B}{H}$$

$$H = \sqrt{\left(\omega L - \frac{1}{\omega C}\right)^2 + R^2}$$

$$\frac{R}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}}$$

$$\frac{R}{Z}$$

$$P_{av} = V_{rms} \times I_{rms} \times \cos \phi$$

$$= I_{rms}^2 \times Z \times \cos \phi \times \frac{R}{Z}$$

$$V_{rms} - I_{rms} Z$$

$$I_{rms}^2 R$$

$$\left(\frac{I_0}{\sqrt{2}}\right)^2 R = \frac{I_0^2}{2} R$$

~~Q~~ factor - The ratio of resonance frequency and band width of a series LCR circuit is known as Q factor of the circuit.

$$Q \text{ factor} = \frac{\text{resonance frequency}}{\text{Band width}}$$

$$Q = \frac{\omega_0}{2\Delta\omega}$$

Expression of Q factor in LCR circuit

$$I_0 = \frac{V_0}{\sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}}$$

for resonance frequency $\omega_0 \cdot I_{max} = \frac{V_0}{R}$

$$I_0 = \frac{1}{\sqrt{2}} I_{max}$$

thus for resonance frequency ω_1, ω_2

$$Z = \sqrt{2} R$$

$$\sqrt{R^2 \left(\omega L - \frac{1}{\omega C} \right)^2} = \sqrt{2} R$$

$$2 \Delta \omega = RL$$

squaring both side

$$R^2 + \left(\omega L - \frac{1}{\omega C} \right)^2 = 2R^2$$

$$\left(\omega L - \frac{1}{\omega C} \right)^2 = R^2$$

$$\left(\omega L - \frac{1}{\omega C} \right) = \pm R$$

$$\omega L = \frac{1}{\omega C} \pm R$$

taking $\omega_2 - \frac{1}{\omega_2 C} = R$

($\omega_2 > \omega$)

$$\omega_2 L - \frac{1}{\omega_2 C} = R \quad (1)$$

taking $-\omega_1 L - \frac{1}{\omega_1 C} = -R$

$$-\omega_1 L - \frac{1}{\omega_1 C} = -R$$

$$\omega_1 < \omega \quad (11)$$

Substituting (1) - (11)

$$(\omega_2 - \omega_1) L + \frac{1}{C} \left(\frac{\omega_2 - \omega_1}{\omega_1 \omega_2} \right) = 2R$$

$$(\omega_2 - \omega_1) \left[L + \frac{1}{C \omega_1 \omega_2} \right] = 2R$$

But in case of resonance

$$\omega_1 = \omega_2 = \omega_0$$

$$\omega_1 \omega_2 = \omega_0^2 = \frac{1}{LC}$$

$$(\omega_2 - \omega_1) \left[L + \frac{1}{C \omega_1 \omega_2} \right] = 2R$$

$$(\omega_2 - \omega_1) \left[L + \frac{1}{C \cdot \frac{1}{LC}} \right] = 2R$$

$$(\omega_2 - \omega_1) \left[L + \frac{LC}{R} \right] = 2R$$

$$(\omega_2 - \omega_1) 2L = 2R$$

$$\omega_2 - \omega_1 = \frac{R}{L}$$

But

$$\omega_2 = \omega_0 + \Delta \omega$$

$$\omega_1 = \omega_0 - \Delta \omega$$

there for Q factor

$$Q = \frac{\omega_0}{2 \Delta \omega} \quad (1)$$

$$= \frac{\omega_0 L}{R}$$

$$= \omega_0 L = \frac{1}{\omega_0 C}$$

$$= Q = \frac{1}{\omega_0 R C}$$

$$\text{but } \omega_0 = \frac{1}{\sqrt{LC}}$$

by eq (1)

$$Q = \frac{1}{\sqrt{LC}} \times \frac{L}{R}$$

$$\frac{1}{R} \times \frac{L}{\sqrt{L} \times \sqrt{C}}$$

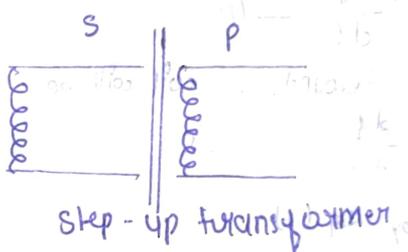
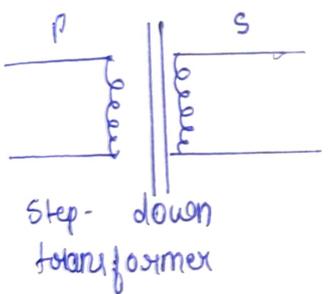
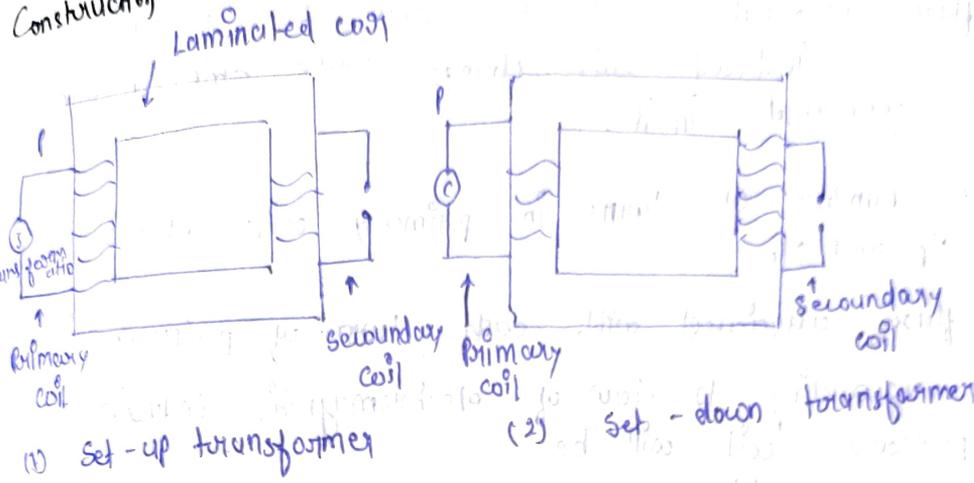
$$\frac{1}{R} \frac{\sqrt{L} \times \sqrt{L}}{\sqrt{L} \times \sqrt{C}}$$

$$Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$

Transformer - Transformer voltage its working is waste on mutual induction core of two type.

- (1) Step-down transformer - This transformer decrease the A.C voltage but increase the value of current.
- (2) Step-up transformer - This transformer increase the A.C voltage but decrease the value of current.

Construction -



Construction - There are mainly three part of transformer

- (i) Laminated core
- (ii) Primary coil
- (iii) secondary coil.

Laminated core - It made up of rectangular or circular strips of pure iron (which are called for middle in the shape of rectangle or circle) these strips are made up of required thickness by giving sufficient layers of varnish. It is called laminated core.

The coil on which alternating voltage is applied is called primary coil and the coil at whose terminal induced emf is obtained is called secondary coil.

In step down transformer, the no. of turns in primary coil are larger and wide is thin in secondary will no. of turns are less and wire is thick.

In primary coil, of step up transformer, turns are less but wire is thick and in secondary coil of step up transformer the no. of turns are greater but the wire is thin.

Working - When alternating voltage is applied between terminal of primary coil then an alternating current flow in the coil. This alternating current produce in coil this alternating magnetic flux associated with secondary coil changes consequently is the induced EMF of same frequency is generated in it.

Theory - Let the number of turns in primary coils and secondary coils are N_p and N_s

If magnetic flux associated with each turn of primary coil is ϕ . then according to law of electromagnetic induction induced in primary coil will be

$$E_p = -N_p \cdot \frac{d\phi}{dt} \quad \text{--- (1)}$$

then induced EMF in secondary coil will be

$$E_s = -N_s \frac{d\phi}{dt} \quad \text{--- (2)}$$

dividing eq (2) by eq (1)

$$\frac{E_s}{E_p} = \frac{N_s}{N_p} \quad \text{by eq (1)}$$

If resistance of primary coil is negligible then induced EMF coil E_p will be equal to applied alternating voltage V_p

Similarly E_s in it will be equal to potential difference V_s between its terminals.

So from eq - (3)

$$\frac{V_s}{V_p} = \frac{N_s}{N_p} \quad \text{--- (4)}$$

$$\frac{N_s}{N_p} = r = \text{transformer ratio} \quad \text{--- (5)}$$

Then input power (power in primary coil) = $V_p \times I_p$

output power (power in secondary coil) = $V_s \times I_s$

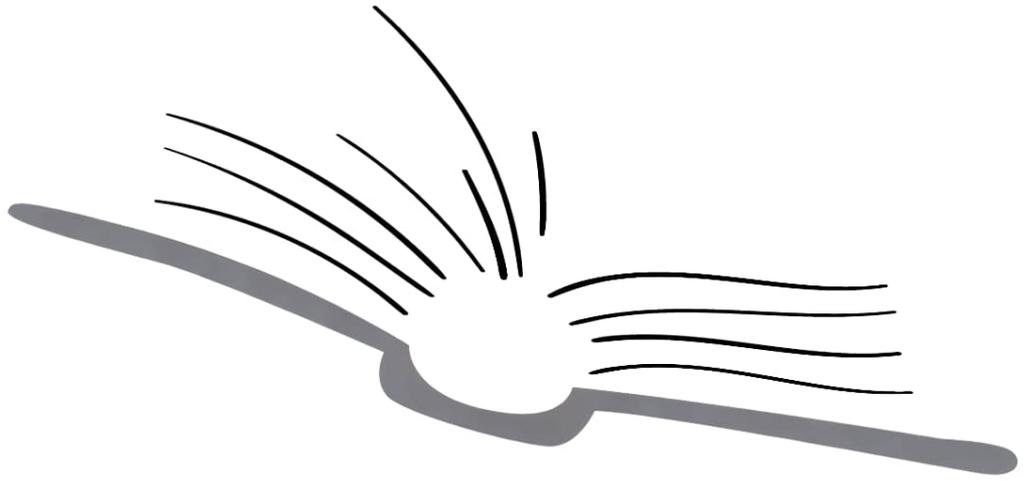
$$\therefore V_p \times I_p = V_s \times I_s$$

$$\text{or } \frac{V_s}{V_p} = \frac{I_p}{I_s} \quad \text{--- (1)}$$

$$\text{or } r_Q \cdot \frac{I}{I}$$

So, from eq 4, 5, 6.

$$\frac{V_s}{V_p} = \frac{N_s}{N_p} = \frac{I_p}{I_s} = \delta$$



THANKYOU
FOR
READIN

